

Starter Problem

1. Use trigonometric identities to transform the left side of the equation into the right side.

$$\frac{\sin \beta}{\cos \beta} + \frac{\cos \beta}{\sin \beta} = \csc \beta \sec \beta$$

2. Use a calculator to evaluate the trig function. Round to four decimal places.

a)  $\sec 56^{\circ}8'10''$

b)  $\cos 56^{\circ}8'10''$

Today's Agenda

1. Starter problems
2. Review assignment due
3. Today's Objectives: You will be able to
  - A) Sketch the graphs of basic sine and cosine functions.
  - B) Use amplitude and period to help sketch the graphs of sine and cosine functions.
  - C) Sketch transformations of sine and cosine functions.
  - D) Use sine and cosine functions to model real-life problems.
4. Today's assignment: 328/15, 16, 22, 24, 28, 35, 42, 60, 74 & 339/1-6, 26, 36, 41, 48, 76
5. **Quiz** 4.1 – 4.3
6. Review for test 4.1 – 4.4

Notes

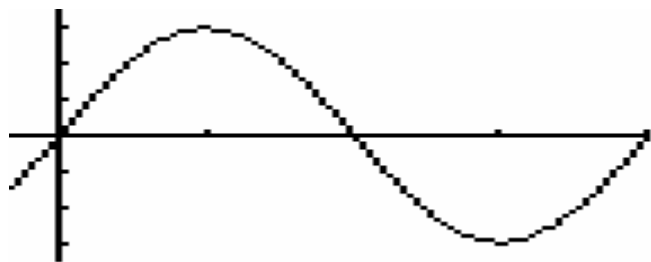
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***Definition of Amplitude of Sine and Cosine***

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The **amplitude** of  $y = a \sin x$  and  $y = a \cos x$  represent half the distance between the maximum and minimum values of the function and is given by:  $\text{Amplitude} = |a|$ .

EX:  $y = 3 \sin x$




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**The minimum is -3 and the maximum is 3 therefore the amplitude = | 3 |.**

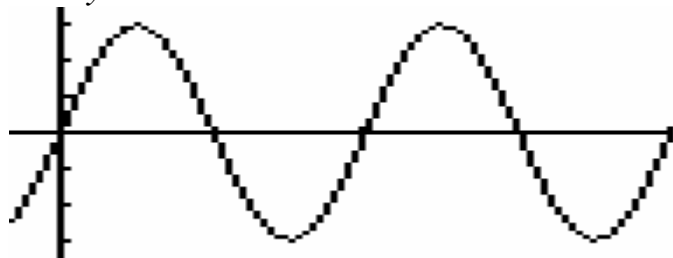
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***Period of Sine and Cosine Functions***

Let  $b$  be a positive real number. The **period** of  $y = a \sin bx$  and  $y = a \cos bx$  is given by

$$\text{Period} = \frac{2\pi}{b}$$

EX:  $y = 3 \sin 2x$



**The amplitude is 3 and the period is  $\pi$ .**

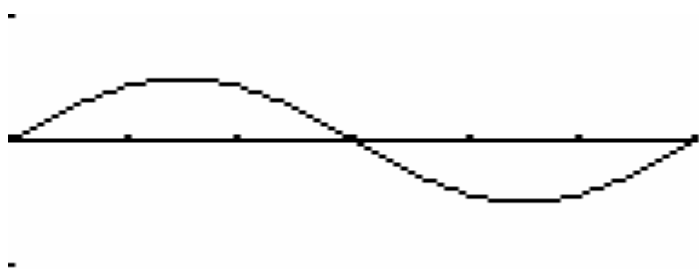
### *Graphs of Sine and Cosine Functions*

The graphs of  $y = a \sin (bx - c)$  and  $y = a \cos (bx - c)$  have the following characteristics.  
(Assume  $b > 0$ .)

$$\text{Amplitude} = |a| \qquad \text{Period} = 2\pi/b$$

The left and right endpoints of a one-cycle interval can be determined by solving the equations  $bx - c = 0$  and  $bx - c = 2\pi$ .

EX:  $y = \frac{1}{2} \sin \left( x - \frac{\pi}{3} \right)$



The amplitude is  $\frac{1}{2}$ . The period is  $2\pi$ . By solving the equations

$$x - \pi/3 = 0 \rightarrow x = \pi/3$$

and

$$x - \pi/3 = 2\pi \rightarrow x = 7\pi/3$$